OPTIMIZATION OF BAFFLE CONFIGURATIONS TO PREVENT AEROACOUSTIC INSTABILITIES IN HEAT EXCHANGERS: PRELIMINARY EXPERIMENTS

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ABSTRACT

It is well known that gas heat exchangers are prone to aeroacoustic instabilities, which often lead to severe noise levels, structural vibrations and fatigue. These are unacceptable, as they threaten the component integrity and expose the plant workers to excessive noise levels. Such phenomenon is due to a cooperative interplay between the Karman vortices generated by the cross-flow and the heat exchanger acoustical modes (mainly those transverse to the tube banks). Energy exchanges are then such that, for certain operating velocities, self-excitation of one or more acoustical modes arises. Actually, this problem is solved by placing rigid baffles inside the container, which modify the acoustic modal fields and eventually inhibit the instability. However, an effective location of such baffles is more or less difficult depending on the system complexity and on the range of flow velocities of interest. For realistic industrial components – using a restricted number of acoustical baffles – their optimal location is a challenging problem, as trial and error experimentation is often a costly and frustrating procedure. In this paper we improve a recently proposed strategy for the optimal location of a given number of baffles, in order to inhibit instability of the acoustical modes in a given frequency range. Our approach is based on a stochastic global optimization technique. Some preliminary experiments are also performed and compared with the simulation results.

1. INTRODUCTION

Gas cross-flows through heat-exchanger tube arrays can severely excite acoustic modes often leading to severe noise levels, structural vibrations and fatigue. This phenomenon is been studied by different authors during the last three decades, see, for instance, (Chen & Young, 1974; Fitzpatrick, 1985; Weaver & Fitzpatrick, 1987). Such phenomenon is mainly due to a cooperative interplay between the vortex-shedding generated by the cross-flow and the heat exchanger acoustical modes, mainly those transverse to the tube banks (Blevins, 1994). Basically the vortex-shedding induced fluctuating lift forces (which are perpendicular to the direction of flow and tube axes) can interact with the particle velocities of the fluid standing waves vibrating in the same direction (Eisinger & Sullivan, 2003). Energy exchanges are then such that, for certain operating velocities, self-excitation of one or more acoustical modes arises. So, an analysis of the fluid excitation forces and of the acoustic modal damping is of prime importance to predict the occurrence of this phenomenon. Unfortunately modeling the acoustic modal damping is a complex task depending on the relative importance of different dissipation mechanisms. These difficulties can be inferred from the compiled literature data showing a notorious dispersion among the representative stability / instability points (Blevins & Bressler, 1980; Laguerre, 1988; Eisinger et al., 1992). Recently Tanaka et al. proposed a new criterion to predict the occurrence of this phenomenon based in an energy balance between the energy of the sound pressure supplied by the fluid flow and the energy consumed by the propagating sound waves (Tanaka et al., 1997; Tanaka et al., 1999). Distinct solutions has been proposed to suppress acoustic resonances (see, for instance, Eisinger, 1980; Blevins & Bressler, 1980; Blevins, 1994). Actually, this problem is solved by placing rigid baffles — see Figures 1 and 2 — inside the container and parallel to the flow stream, which modify the acoustic...
modal fields and eventually inhibit the instability (see, for instance, (Eisinger & Sullivan, 2003; Eisinger & Sullivan, 2004; Fenstra & Weaver, 2004). Observe that, contrary to common belief and what has often been stated, typical baffles only change acoustic frequencies marginally because the acoustic space remains connected up-steam and downstream of them. Its main effect is to distort the acoustic modes decreasing the corresponding susceptibility to aeroacoustic instability (Eisinger & Sullivan, 2003). A general procedure, based on acoustic particle velocity mode shape functions, to evaluate the acoustic baffle effects was recently developed by Eisinger & Sullivan, 2003. This procedure involves the energy analysis of the oscillation energy provided by the vortex lift forces when the vortex shedding frequency approach modal frequencies, for both the original mode shapes of the system without baffles and the acoustic mode shapes distorted by the baffles, as well as the determination of the corresponding parameters extracted from experimental data.

In this work we improve the functional $\mathfrak{F}$ recently proposed (Moreira et al., 2006) to estimate the susceptibility to aeroacoustic instability of the various modes in a given frequency range. A simulated annealing (see, Moreira et al., 2007) procedure is then implemented to minimize $\mathfrak{F}$ and obtain an appropriate $M$-baffle configuration. Some preliminary experiments are performed and compared with the simulation results.

2. THEORETICAL CONSIDERATIONS

Consider a rectangular flow channel containing some tube banks shown in Figure 1, which represents a typical re-heater from a power station boiler. Following (Tanaka et al., 1997; Tanaka et al., 1999), consider the forced modal acoustic pressure equations for a generic cavity

\[ \ddot{p}_n(t) + 2\zeta_n\omega_n\dot{p}_n(t) + \omega_n^2p_n(t) = \epsilon^2 \int_V \mathbf{F} \cdot \nabla \varphi_n \, dv, \quad n = 1, 2, \ldots \]  

(1)

where $\dot{p}_n(t,x,y) = p_n(t)\varphi_n(x,y)$ stands for $n^{th}$-modal acoustic pressure amplitude, $\mathbf{F}$ the acoustic forcing field, $\omega_n$ the acoustic $n^{th}$-modal angular frequency, $\zeta_n$ the $n^{th}$-modal reduced damping and $c$ is the sound velocity. Note that, for simple domains, the acoustical modes may be obtained analytically (apart from damping). For realistic heat-exchangers, the acoustic modes are computed using finite elements (Cook et al., 2002). The acoustical effects of the tube banks may be conveniently accounted using an equivalent sound velocity, as discussed later, obtained from an homogeneous model of the acoustic field (Parker, 1978).

Note that integrations are performed in the interest regions, namely $V$ is the complete acoustical domain and $T$ is the subdomain occupied by the tube banks, where the vortex excitation arises. From (1) these authors deduced that, when the vortex generated forces are fully correlated with the acoustical mode $\varphi_n$, one can express the modal forcing pressure source $p_n$ as

\[ p_n = K_n \int_T \left( \nabla \varphi_n \right)^2 \, dv \int_V \varphi_n^2 \, dv, \quad n = 1, 2, \ldots \]  

(2)
where $K_n$ is an appropriate complex factor depending on the bundle geometry as well as the main flow characteristics.

Note that, for a straight rectangular duct with uniform flow and acoustic conditions, it is well documented by experimental results that the vortex-shedding excitation correlates particularly well with the acoustical responses which are mainly transverse to both the tubes and the flow. This fact justifies why the acoustic modes typically excited by crossflow in tubular heat exchangers tube banks are transverse modes (see, Eisinger & Sullivan, 2003). Therefore, the forcing pressure source $p_n$ expression (2) will be here, tentatively, approximated as

$$p_n \approx K_n \int_T \left( \frac{\partial \varphi_n}{\partial y} \right)^2 dv, \quad n = 1, 2, \ldots$$

This means that, in order to minimize the system susceptibility to aeroacoustic instability we must minimize (3), in a given frequency range (related to the Strouhal shedding frequencies excited by the flow velocity of interest), say $\Omega_1 \leq \omega_n \leq \Omega_2$, using an optimal configuration of a number of baffles in the flow channel. Notice that most of the complex physics of the vortex excitation and aeroacoustic interaction are encapsulated in the modal parameters $K_n$. For their determination one usually has to perform extensive experimentations, as they are in general frequency dependent complex quantities. Here, however, we will assume for simplicity that the acoustical mode shapes are a dominant factor which controls the acoustical modal susceptibility to aeroacoustic instability supposing additionally that $K_n \ll 1/\omega_n^2$.

From the above-mentioned arguments one may propose the following improved (see, Moreira et al., 2006) functional to minimize

$$F \{ B_i, i = 1, \ldots, M \}$$

$$= \max_n \left\{ \int_T \left( \frac{\partial \varphi_n}{\partial y} \right)^2 dv \right\}$$

over the appropriate frequency range of interest, $\Omega_1 \leq \omega_n \leq \Omega_2$. Here, integrations are respectively, performed in the tube banks region ($T$-region) or in the complete domain ($V$-region), respectively. Observe that $\{ B_i, i = 1, \ldots, M \}$ stands for a given $M$—baffle configuration, which distorts the pressure mode shapes in the frequency range of interest.

### 3. Optimization Strategy

The minimization of functional (4) involves the computation of the modal frequencies and cavity pressure mode shapes for each given $M$—baffles configuration. This task is performed with a set of algorithms developed by the authors using the Matlab PDE Toolbox (Partial Differential Equation Toolbox) which automatically generates the geometry and the finite element mesh (corresponding to the given $M$—baffles configuration) and then computes the modes from the Helmholtz equation. The boundary conditions used are Neumann in the axial walls and Dirichlet at the inlet and outlet of the duct. Then for each mode we compute $\int_T \left( \frac{\partial \varphi_n}{\partial y} \right)^2 dv$ and

$$\int_V \varphi_n^2 dv$$

in order to find the excitation susceptibility function $F \{ B_i, i = 1, \ldots, M \}$ in the given frequency range of interest.

For minimization of (4), we adopted the basic simulated annealing strategy described in Press et al., 1997, based in the Metropolis algorithm (Metropolis et al., 1953). Roughly speaking, simulated annealing is a global minimization strategy based on an analogy to the annealing of metals, in which a slow cooling (anneal) of a previously heated metal gives it more chances of finding structure configurations with lower internal energy than the initial one.

The algorithm consists in, for a given $M$—baffle configuration $\{ B_i, i = 1, \ldots, M \}$ and for an appropriately chosen temperature $T$, generate a random perturbation of the positions of the $M$ baffles. The new perturbed $M$—baffle configuration $\{ \tilde{B}_i, i = 1, \ldots, M \}$ will be accepted as better than the original one if $F \{ B_i, i = 1, \ldots, M \} \geq F \{ \tilde{B}_i, i = 1, \ldots, M \}$. If $F \{ B_i, i = 1, \ldots, M \} < F \{ \tilde{B}_i, i = 1, \ldots, M \}$ the new perturbed $M$—baffle configuration $\{ \tilde{B}_i, i = 1, \ldots, M \}$ will be accepted with a probability $p$, computed as

$$p = \exp \left( \frac{-F \{ \tilde{B}_i, i = 1, \ldots, M \} - F \{ B_i, i = 1, \ldots, M \}}{T} \right).$$

Therefore, local minima may be overcome through (5). Notice that, the probability of acceptance worst solutions decrease as temperature $T$ is lowered, so that the algorithm progressively focus on a narrower search domain.

Generically, it can be shown that the iteration of this strategy for any given finite problem, using an infinitely slow decreasing temperature schedule $T$, generates a sequence of configur-
tions which approach a global optimal solution (see for instance, Arst & Korst, 1989). However, in practical implementations of simulated annealing, finding a global optimal solution (in a finite time) is not guaranteed in general. Nevertheless, as in many other fields, our implementation proved successful and well suited in the context of the problem addressed here.

4. NUMERICAL RESULTS

All the performed numerical computations were based on the rectangular flow channel schematically represented in Figure 2. The main geometric parameters are shown in Table 1, pertaining to an experimental rig currently under testing (see Figure 1).

Observe that the position of tube bundles are defined by the tabulated parameters $L_1, \ldots, L_{11}$. According to Table 1, the main geometrical parameters are as follows:

<table>
<thead>
<tr>
<th>$L_X$ [m]</th>
<th>$L_Y$ [m]</th>
<th>$L_1$ [m]</th>
<th>$L_{2,4,8,10}$ [m]</th>
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<tr>
<td>0.414</td>
<td>0.206</td>
<td>0.096</td>
<td>0.026</td>
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<tr>
<th>$L_{3,5,7}$ [m]</th>
<th>$L_6$ [m]</th>
<th>$L_9$ [m]</th>
<th>$L_{11}$ [m]</th>
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<tr>
<td>0.014</td>
<td>0.056</td>
<td>0.05</td>
<td>0.006</td>
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</table>

<table>
<thead>
<tr>
<th>$L_A$ [m]</th>
<th>$L_B$ [m]</th>
<th>$P$ [m]</th>
<th>$D$ [m]</th>
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<tr>
<td>0.030</td>
<td>0.028</td>
<td>0.010</td>
<td>0.006</td>
</tr>
</tbody>
</table>

Table 1: Main geometrical parameters.

As discussed before, the estimation of the sound velocity $c$ in regions with tubes was based in the corrective expression (see, for instance, Blevins & Bressler, 1980)

$$c = c_0 \frac{1}{\sqrt{1 + \sigma}},$$

where $c_0$ is the sound velocity in air and $\sigma = 0.7853 \left( \frac{D}{P} \right)^2$. Note that the tabulated $D$ and $P$ values stand for the tube diameter and pitch for the corresponding square-arranged tube banks.

The baffles used in computations are 0.08 m long and 0.002 m thick. Note that, the possible $y-$coordinate positions of the baffles were defined by the tabulated $L_A$ and $L_B$ values. This means that the possible configuration space of a given $M$ baffles is discrete in the $y-$direction.

In order to be able to address a significant number of higher order transverse modes we choose the frequency range of interest to be $0 \sim 2000$ Hz.

In Table 2, we display the reference value of the susceptibility function (4), for our system with no baffles $F \{\emptyset\}$, as well as the corresponding baffle locations and values of the minimized susceptibilities using 1 and 2 baffles.

In Figure 3 a) we display the acoustic mode shape of the frequency with largest susceptibility for our system with no baffles. In Figures 3 b) and 3 c) we display the corresponding acoustic mode shapes of the frequency with largest susceptibility with respect to the corresponding computed optimum configuration.

Observe, in first place, that the susceptibility function $F$ decreases when the number $M$ of optimum located baffles is increased as it should (see, Table 2).

The largest modal susceptibility with respect the corresponding configuration occur in the first transverse pressure mode shape at 824 Hz [see,
Figure 3 a)]. One can note the distorting effects, of the baffles, over the mode shapes modifying the orientation of the transverse components of the acoustic pressure gradient (see, Figures 3 b) and 3 c). One can estimate that the corresponding frequencies were modified by the baffles 10% ~ 20%. This fact is in agreement with Eisinger et al., 2003.

5. EXPERIMENTS

Experiments were performed in the test rig shown in Figure 1. The working fluid is air flowing through our test rig with an intertube speed of about 20 m/s. The acoustical pressure amplitude \( p \) and frequency \( f \) are measured at the open outlet of the test rig by means of a sound level meter Brüel&Jær type 2221. The transmitter output is connected to the port of a Spectral Dynamic acquisition board (Model 20-42) which ensures the analog digital conversion.

In Figure 4 we display the autospectra of our system for the intertube air speed of 20 m/s, with no baffles as well as 1 and 2 baffles localized in the optimum positions displayed in Table 2.

We observe that the noise level \( \text{Leq} \) decreases (0 baffles: 103.5 dB; 1 baffle: 91.6 dB; 2 baffles: 84.2 dB) when the number \( M \) of optimum located baffles is increased showing that the instability occurring at 824 Hz [see Figure 4 a)] was effectively inhibited [see Figure 4 c)]. Note also that the frequency of the unstable mode shape were modified by the presence of the first baffle less than 10%.

6. CONCLUSIONS

In this paper we presented a systematic approach to optimize \( M \)-baffle configurations, in order to inhibit aeroacoustic instabilities in heat exchanger tube banks caused by vortex shedding. A stochastic global optimization method has been implemented to compute optimal baffle locations, in order to minimize a given functional which reflects the system susceptibility to aeroacoustic instabilities. A tentative configuration-dependent functional recently adopted was improved. This functional (see, Moreira et al. 2006) was based on physical ideas borrowed from Tanaka et al., 1997 and Eisinger & Sullivan, 2003. The spatial aspects of the force field and of the acoustic modes were considered totally correlated when aeroacoustic instability arises - have been considered the dominant factor which triggers (or not) the unstable behavior. Additionally the complex physics of the vortex excitation and aeroacoustic interaction, considered encapsulated in the modal parameters \( K_n \), was assumed satisfying \( K_n \ll 1/\omega_n^2 \).

A realistic test case was presented, for which the optimal baffle configurations - using 1 and 2 baffles - were computed. The results obtained when no baffles are used were compared with those stemming from the optimal baffle configurations. They clearly show a significant decrease of the system modes susceptibility to aeroacoustic instabilities when one or more baffles are optimally located. Furthermore, as expected, such susceptibility further decreases as the number of baffles is increased.

The theoretical results obtained was compared with preliminary experiments showing a satisfactory agreement.

Indeed, the proposed approach present an obvious interest, both as a tool for designing quiet heat exchangers as well as for fixing problems in actual components.

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8. REFERENCES


