Electromagnetic and Thermal Aspects of a Fast Field Cycling NMR Equipment

Magnet and Power Supply

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Abstract—The Fast Field Cycling Nuclear Magnetic Resonance (FFC-NMR) technique has been spreading its application to new areas such as oil and food industry. Consequently, new features and improvements concerning the equipment available have been investigated and exploited. Under this context, this paper describes the main aspects concerning the electromagnetic and thermal behavior of the main power supply and the magnet, respectively. The proposed power supply and the magnet were developed under the specifications of the FFC-NMR equipment and in order to match the requirements of the most recent areas of application. The dynamic behavior of the power supply is analyzed based on simulation results, being the thermal study of the magnet performed using finite element method software.

Keywords—Spectrometer; Power Supply; Magnet; Nuclear Magnetic Resonance; Fast Field Cycling; Thermal Study

I. INTRODUCTION

The Fast Field Cycling Nuclear Magnetic Resonance (FFC-NMR) is an experimental technique used to study the molecular dynamics of different types of compounds. This technique has a high use in various research areas such as Physics, Chemistry, Medicine, and Pharmacy, among others. This technique requires relaxometers that allow switching the magnetic flux density quickly, accurately and in a repetitive way. As first approach, the switching times are within the millisecond range and maximum magnetic flux density is 0.2T [1-3].

In Fig. 1, the main blocks of a NMR spectrometer are represented. Among other circuits and components, a FFC-NMR needs a specific magnet and a fast suitable power supply. The power supply is a current source, which must allow rapid transitions of the current, i.e., switching the current between 0 and 10 A within the time range 3 to 6 ms (t_on and t_off, see Fig. 2). Furthermore, the current ripple should be as low as possible in order to guarantee an accurate magnetic flux density \( B_0 \) and a very high homogeneity given by the expression (1) [4].

\[
\frac{\Delta B}{B_0} = \frac{B_{\text{max}} - B_{\text{min}}}{B_0}
\]  

(1)

The Fast Field Cycling technique is used to determine the longitudinal relaxation time \( T_1 \) over a range of the magnetic flux density not covered by classical NMR techniques. In this work, the proposed solution covers a flux density range from 0 T to 0.4 T, corresponding to a magnet current range from 0 to 10A, as referred before. Doubling the maximum magnetic flux density, the proposed power supply and magnet will contribute to expand the range and type of samples that can be studied with this technique.


df. 1. Main blocks of a FFC NMR spectrometer

FFC magnets are designed according a target flux density \( B_0 \). In general the homogeneity of the magnetic flux density is

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Considered the most important requirement for the magnet [1-2,5], however, it should also have minimum power losses.

FFC-NMR spectrometers have been evolving, taking advantage of the evolution of power electronics devices and magnet design techniques.

In this paper, a different solution for the power supply of the FFC-NMR spectrometer is described and simulated. The main results concerning the temperature distribution in the magnet are also shown.

II. THE POWER SUPPLY

During a normalized FFC-NMR experiment the magnetic flux density cycles as represented in Fig. 2. During a cycle, the following stages are observed:

1. The sample is polarized with a high magnetic flux density \( B_{0p} \) (polarization field) during a time interval \( \Delta t_p \), until the nuclear magnetization of the sample achieves saturation, i.e., \[ \Delta \mathcal{M} = 5 \mathcal{M}_0(\delta \mathcal{M}/\delta t) \]

2. The magnetic flux density is switched to a value \( B_{0e} \) (evolution field), lasting at this level for a time \( \Delta t_e \) during which the nuclear magnetization relaxes towards a new equilibrium value.

3. The magnetic flux density is switched to a value \( B_{0d} \) (detection field) and the sample is excited by the RF pulse. The sample’s response is detected and acquired by the RF unit tuned to a predetermined frequency respecting the Larmor frequency of the molecular element under study. After cessing the RF pulse is detected the signal (FID - Free Induction Decay), that is used to determine \( T_1 \).

The polarization field \( (B_{0p}) \) and detection field \( (B_{0d}) \) may have different values, being usually \( B_{0p} \geq B_{0d} \) [1-2,6].

The project of a power supply for a FFC-NMR magnet includes several requirements and can be based on different assumptions. The magnet current should behave as a current source allowing fast current switching times in order to obtain a magnet flux density cycling as represented in Fig. 2 [7-8]. In this work, it is also assumed that the characteristic magnetic flux density vs. magnet current is linear and that the power supply should contribute to get fast magnet current transients.

The power supply should be able to control the magnet current from 0 to 10A and the response times of the current transitions within the range 3 to 6 ms.

The design of the magnet influences the project of the power supply, mainly their electric resistance, \( R_m \) and self-inductance \( L_m \). In this paper was considered a magnet developed recently [9] with self-inductance of 0.2 H and electrical resistance of 3\( \Omega \).

When setting up the power supply topology, it should be considered fully controllable semiconductor, i.e., it should be considered the possibility of controlling the operating point of the semiconductors in addition to the typical "ON" and "OFF" states.

A. Electric circuit

The circuit shown in Fig. 3 represents the proposed power supply. This circuit is constituted by two voltage sources \( V \) and \( V_{aux} \), diodes \( D \), \( D_{aux} \), \( D_{RL} \) and a switches IGBTs \( S \) and \( S_{aux} \) and a RC filter \( C \) and \( R_L \), being the load the magnet with parameters \( R_m \) and \( L_m \). To analyze the dynamic behavior and the operating principles of this circuit, 3 operating modes are considered:
- steady state;
- "up" transient; and
- "down" transient.

Fig. 3. Electric circuit of the power supply

1) Steady State:
In steady state (current regulated), \( V_{aux} \) remains disconnected (\( S_{aux} \) is “OFF”), being the equivalent circuit represent by Fig. 4.

Fig. 4. Electric circuit in steady state

If the semiconductor \( S \) is "ON", the current flows from the voltage source \( V \) to the magnet, being the diode \( D_{RL} \) “OFF".
During this process, the capacitor $C$ discharges through the resistor $R_C$. Neglecting the voltage drop of the semiconductors (switch and diode), in steady state the magnet current is regulated knowing that:

$$I_m = \frac{v}{R_m} \left( 1 - e^{\frac{-R_m}{L_m}} \right)$$  \hfill (3)

If $S$ is “OFF”, the energy stored in the coil will be transferred to the capacitor. During this transition the energy is dissipated in the resistance $R_m$. However, the amount of energy transferred from the inductor to the capacitor is very small, since the purpose is to keep the current constant.

2) “Up” transient:

In Fig. 5, it is shown the equivalent circuit during the “up” transient.

![Electric circuit for the “up” transient](image)

During the “up” transient the semiconductor $S_{aux}$ is “ON” ($S$ is “OFF” avoiding short-circuiting the voltage sources). The control systems is designed to detect when the magnet current reaches the target current level, switching $S_{aux}$ “OFF” and changing the operation mode to “steady state”.

The time evolution of the magnet current is:

$$I_m = \frac{V_{aux}}{R_m} \left( 1 - e^{\frac{-R_m}{L_m}} \right)$$  \hfill (4)

Since $V_{aux}>>V$, the magnet current dynamics is accelerated in order to fulfill the requirements of the application.

3) “Down” transient:

During the “down” transient the magnet current path is represented in Fig. 6.

![Electric circuit for the “down” transient](image)

According to Fig. 6, during the “down” transient the energy stored in the magnet is transferred to the capacitor $C$. Since the impedance of the resistance is much higher than the impedance of the capacitor ($Z_{RC}>>Z_C$), the current flows through the diode $D_{RL}$ being neglected the current flowing through the resistor $R_C$.

In this situation it is intended that the current drops very fast, so the amount of energy transferred from the inductor to the capacitor is large. The energy transfer rate is responsible for decreasing the magnet current as fast as possible.

When the current reaches the reference value, the semiconductor $S$ is set to “ON” and the system goes into steady state, again.

### III. CONTROL SYSTEM

In Fig. 7, the circuit with a closed loop control chain is shown. A core point is the design of the magnet current regulator. In Fig. 8 the block diagram of the proposed solution in order to set the regulator parameters is represented.

![Diagram of the circuit with the regulation chain](image)

In Fig. 8, the block $C(S)$ represents the regulator, the central block represents the dynamic model of the switched converter, being $T_a$ a time constant related with the statistical delay caused by characteristic delays in the command system and $K$ is the gain of the converter. The third block represents the transfer function of the magnet.

A PI (proportional and integral action) controller is used to control the circuit, ensuring a fast response and a null static error. Being the typical transfer function of the PI controller:

$$C(s) = \frac{K_P + \frac{K_I}{s}}{1 + s T_a}$$

To determine the regulator parameters ($K_P$ and $K_I$) the modulus optimum technique is used [10]. This technique cancels the dominant pole of the load with a zero of the regulator, i.e., the time constant $T_Z$ is given by:

$$T_Z = \frac{1}{s K_P + K_I}$$  \hfill (5)
\[ T_Z = \frac{l_m}{R_m} \quad (6) \]

Taking into account (6), the global transfer function of the system can be represented by:

\[ \frac{T_m(s)}{T_{Ref}(s)} = \frac{1}{sT_p + 1} \frac{K}{s^2 + \frac{1}{T_a} + \frac{1}{T_a R_m}} = \frac{K}{s^2 + \frac{1}{T_a} + \frac{1}{T_a R_m}} \quad (7) \]

For this type of system, the static speed error should be minimized. Using the ITAE criteria, the 2nd order optimized transfer function is given by [10-11]:

\[ F(s) = \frac{\omega_n^2}{s^2 + \sqrt{2} \omega_n s + \omega_n^2} \quad (8) \]

Considering (7) and (8), the following expressions, under optimized conditions, are obtained:

\[ \omega_n^2 = \frac{K}{T_a R_m} \]
\[ \sqrt{2} \omega_n = \frac{1}{T_a} \quad (9) \]

Solving the previous equation system:

\[ T_p = \frac{2 K T_a}{R_m} \quad (10) \]

The proportional and integral gains, can be estimated using:

\[ K_I = \frac{1}{T_p} \quad (11) \]
\[ K_P = \frac{T_a}{t_p} \quad (12) \]

The current error is given by:

\[ E(s) = I_{Ref} - I_m(s) = I_{Ref}(s) \frac{s T_p (1 + s T_a) R_m}{s T_p (1 + s T_a) R_m + K} \quad (13) \]

By the final value theorem, taking into account that the reference is a step (\( I_{Ref}(s) = 1 / s \)) it can be verified that the static error is null:

\[ \lim_{s \to 0} s E(s) I_{Ref}(s) = \frac{0}{K} = 0 \quad (14) \]

IV. SIMULATION RESULTS

The proposed solutions for the power supply together with the control system are analyzed by simulation. In Fig. 9 the simulation model is represented. The block "Selector" is responsible for selecting the operation mode avoiding short-circuits between the voltage source \( V \) and the auxiliary voltage source \( V_{aux} \) (a dead time is considered between the sequences "OFF" – "ON" of the switches).

To compute the simulations a regulator with the following gains is considered:

- \( K_P = 1 \);
- \( K_I = 15 \);
- \( K_I = 1 \).

![Simulation model of the power supply](image_url)

The simulation results are obtained having as reference the normalized field cycle (Fig. 2). The reference current waveform is set with parameters that are typical of a real FFC experiment. The current levels \( I_D \) and \( I_E \) are proportional to the flux density levels \( B_{0D} \) and \( B_{0E} \), respectively.

The parameters used are:

- \( I_D = 10 \) A;
- \( I_E = 4 \) A;
- \( t_{on} = 3 \) ms;
- \( t_{off} = 6 \) ms.

In Fig. 10 the simulation result of the magnet current is shown. In Fig. 11 and Fig. 12 the “up” and “down” transients are illustrated, respectively. To perform the simulations the values of other parameters are:

- \( V = 50 \) V;
- \( V_{aux} = 400 \) V;
- \( C = 147 \) µF;
- \( R_C = 280 \) Ω.

![Simulation result of the magnet current](image_url)

Fig. 10. Simulation result of the magnet current: a) reference current; b) magnet current
The \( C \) value was designed considering the power stored in the magnet \((W_L)\) and the voltage variation \((\Delta v_C)\) that is observed when during a current \(^\text{“down”}\) transient, i.e., \( C = \frac{1}{2} W_L \frac{1}{\Delta v_C} \). For other hand, \( R_C \gg (1/\omega C) \) in order to obtain the required system dynamics.

In Fig. 13 it is shown the simulation result for an enlarged current cycle. In Fig. 14, the current ripple corresponding to the different current levels set to the enlarged cycle is shown.

The simulation results allow verifying that the current dynamics fulfills the requirements of the application. For other hand, the current ripple for the maximum current \((10A)\) can be seen as a drawback of the proposed solution. Anyway, the ripple could be reduced increasing the switching frequency of the semiconductors.

V. THERMAL STUDY OF THE MAGNET

The magnet designed to be used with the proposed power supply is shown in Fig. 15. This magnet is based on a ferromagnetic core with two set of coils placed in the central leg, which has an air-gap where the sample submitted to a FFC NMR experiment is placed.
To evaluate the magnet temperature distribution, a study is performed using a 2D finite element software (FEMM). An example of the output obtained with these simulations is shown in Fig. 16.

![Temperature distribution in the magnet](image)

Fig. 16. Temperature distribution in the magnet

According to the temperature distribution observed, there is a standard behavior that allows getting the average temperature for the three main parts of the magnet: ferromagnetic core, windings and air gap. In Table I the average temperature for these three points for different values of the power losses is shown, which are the main heat source of this system.

The results summarized in Table I, point out clearly that the magnet requires forced ventilation. In Table II are summarized the temperatures, for the same points, with ventilation. The real magnet is encapsulated including a fan that cools the magnet extracting the air contacting the hot parts of this system.

<table>
<thead>
<tr>
<th>TABLE I.</th>
<th>TEMPERATURES INSIDE THE MAGNET WITHOUT FORCED VENTILATION</th>
</tr>
</thead>
<tbody>
<tr>
<td>$P_{losses}(W)$</td>
<td>$T_{windings}(°C)$</td>
</tr>
<tr>
<td>100</td>
<td>53.85</td>
</tr>
<tr>
<td>200</td>
<td>83.65</td>
</tr>
<tr>
<td>300</td>
<td>113.55</td>
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<tr>
<td>400</td>
<td>143.35</td>
</tr>
<tr>
<td>500</td>
<td>173.15</td>
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</table>

<table>
<thead>
<tr>
<th>TABLE II.</th>
<th>TEMPERATURES INSIDE THE MAGNET WITH FORCED VENTILATION</th>
</tr>
</thead>
<tbody>
<tr>
<td>$P_{losses}(W)$</td>
<td>$T_{windings}(°C)$</td>
</tr>
<tr>
<td>100</td>
<td>30.95</td>
</tr>
<tr>
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<tr>
<td>400</td>
<td>51.65</td>
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<tr>
<td>500</td>
<td>58.55</td>
</tr>
</tbody>
</table>

The analyzed system allows obtaining a magnetic flux density up to 0.4 T (corresponding to a magnet current of 10A). This magnetic flux density level allows setting the FFC equipment, not only with the proton specifications, but also considering fluorine atoms.

The designed magnet matches with the proposed solution for the power supply. This magnet is portable (important advantage than other FFC magnets) and can be cooled by a simple fan.

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**REFERENCES**


